

Exhibit A

Rim material: Glass Fiber / Epoxy matrix

1. Modulus of elasticity E_r in the hoop direction is calculated by Equation 5.3, shown in Attachment 1, which gives the E_r value of the composite based on the volume fraction of fiber and matrix.

$$E_r = E_c = V_f E_f + E_m (1 - V_f) \quad (5.3)$$

The volume fraction of fiber is known by the flywheel manufacturer using convention measurement techniques. In this example, the fiber volume fraction

$$\begin{aligned} V_f &= 0.65 \\ E_m &= 413 \text{ ksi (from Attachment 2)} \\ &= 2.85 \text{ GPa} \\ E_f &= 72.45 \text{ GPa (from Attachment 3, page 2)} \\ E_r &= 0.65 \times 72.45 + 2.85 \times (1 - 0.65) \\ &= 48.09 \text{ GPa} \end{aligned}$$

Rim liner material: Nylon 66

2. $E_l = 3.5 \text{ GPa}$ (from Attachment 4)

3. To obtain the ratio R_r of hoop modulus to density E_r/ρ_r , the density ρ_r is calculated from Equation (5.6) in Attachment 1 as follows:

$$\begin{aligned} \rho_r &= \rho_c = V_f \rho_f + V_m \rho_m \\ &= V_f \rho_f + (1 - V_f) \rho_m \\ \rho_f &= 2.59 \text{ g/cm}^3 = 2.59 \times 10^3 \text{ Kg/m}^3 \text{ (from Attachment 3)} \\ V_f &= 0.65 \\ \rho_m &= 1.161 \text{ g/cm}^3 = 1.161 \times 10^3 \text{ Kg/m}^3 \text{ (from attachment 2)} \\ \rho_r &= 0.65 \times 2.59 \times 10^3 + (1 - 0.65) \times 1.161 \times 10^3 \\ &= 2.09 \times 10^3 \text{ Kg/m}^3 \end{aligned}$$

$$\begin{aligned} R_r &= E_r / \rho_r \\ R_r &= 48.09 / (2.09 \times 10^3) \\ &= 0.23 \text{ GPa m}^3/\text{Kg} \end{aligned}$$

4. To obtain the ratio R_l of hoop modulus to density E_l/ρ_l , the density of the liner material can be obtained from open literature. In this case, the density of Nylon 66 is

$$\begin{aligned} \rho_l &= 1.14 \times 10^3 \text{ Kg/m}^3 \quad \text{(from Attachment 4)} \\ R_l &= E_l / \rho_l \\ &= 3.5 / (1.14 \times 10^3) \\ &= 0.0031 \text{ GPa m}^3/\text{Kg} \end{aligned}$$

Therefore, $R_r > R_l$